

# APPENDIX ONE

## Constructing Problem Sets

The function TEST runs all problems in the list *\*problems\**. The contents of *\*problems\** can be set by loading one of the problem-sets provided, or the user can construct new problem-sets. A problem-set is a list of problems, where a problem is a list of the following:

1. problem-number
  2. a list of premises, which are triples (formula, supposition, degree-of-justification)
  3. a list of desired conclusions, which are pairs (formula, degree-of-interest)
  4. a list of forwards prima facie reasons, which are quintuples (name,premises,conclusion,variables,strength)
  5. a list of forwards conclusive reasons, which are quadruples (name,premises,conclusion,variables)
  6. a list of backwards prima facie reasons, which are sextuples (name,forwards-premises,backwards-premises,conclusion,variables,strength)
  7. a list of backwards conclusive reasons, which are quintuples (name,forwards-premises,backwards-premises,conclusion,variables)
  8. an optional string describing the problem.
- All formulas can be entered as pretty formulas instead.

For example, the following is a problem:

```
(2
(("P" nil 1) ("A" nil 1))
(("R" 1))
(("pf-reason 1" ("P" is-inference)) "Q" nil 1)
("pf-reason 2" ("Q" is-inference)) "R" nil 1)
("pf-reason 3" ("A" is-inference)) "B" nil 1)
(("con-reason 1" ("G" is-inference)) "J" nil 1)
("con-reason 2" ("E" is-inference)) "H" nil 1)
("con-reason 3" ("H" is-inference)) "K" nil 1)
("con-reason 4" ("F" is-inference)) "I" nil 1)
("con-reason 5" ("F" is-inference)) "(B @ E)" nil 1)
("con-reason 6" ("H" is-inference)) "(D @ G)" nil 1)
(("pf-reason 4" nil ("C" nil)) ("~" "R") nil nil 1)
("pf-reason 5" nil ("B" nil)) ("C" nil) nil 1)
(("con-reason 7" nil ("F" nil)) ("~" "S") nil nil 1)
("con-reason 8" nil ("G" nil)) ("V" nil) nil 1)
"This is a hard problem.")
```

This list of problems in *\*problems\** can be displayed in a more perspicuous form by running (DISPLAY-PROBLEMS). For example, if *\*problems\** is the list consisting of just the above problem, this produces the following display:

```
Problem #2
This is a hard problem.
Given premises:
  P   justification = 1
  A   justification = 1
Ultimate epistemic interests:
  R   intere
FORWARDS PRIMA FACIE REASONS
pf-reason 1: {P} ||=> Q strength = 1
pf-reason 2: {Q} ||=> R strength = 1
pf-reason 3: {A} ||=> B strength = 1

FORWARDS CONCLUSIVE REASONS
con-reason 1: {G} ||=> J strength = 1
con-reason 2: {E} ||=> H strength = 1
```

```

con-reason 3: {H} ||=> K strength = 1
con-reason 4: {F} ||=> I strength = 1
con-reason 5: {F} ||=> (B @ E) strength = 1
con-reason 6: {H} ||=> (D @ G) strength = 1

```

BACKWARDS PRIMA FACIE REASONS

```

pf-reason 4: {} {C} ||=> ~R strength = 1
pf-reason 5: {} {B} ||=> C strength = 1

```

BACKWARDS CONCLUSIVE REASONS

```

con-reason 7: {} {F} ||=> ~S strength = 1
con-reason 8: {} {G} ||=> V strength = 1

```

Problems can also be entered in this more perspicuous form, using the function MAKE-PROBLEM-LIST. For example, executing

```

(setf *problems* (make-problem-list
"Problem #1
This is a case of collective rebutting defeat
Given premises:
P justification = 1
A justification = 1
Ultimate epistemic interests:
R interest = 1

```

FORWARDS PRIMA FACIE REASONS

```

pf-reason 1: {P} ||=> Q strength = 1
pf-reason 2: {Q} ||=> R strength = 1
pf-reason 3: {C} ||=> ~R strength = 1
pf-reason 4: {B} ||=> C strength = 1
pf-reason 5: {A} ||=> B strength = 1

```

Problem #2

This is the same as #1 except that some reasons are backwards.

Given premises:

```

P justification = 1
A justification = 1

```

Ultimate epistemic interests:

```

R interest = 1

```

FORWARDS PRIMA FACIE REASONS

```

pf-reason 1: {P} ||=> Q strength = 1
pf-reason 2: {Q} ||=> R strength = 1
pf-reason 3: {A} ||=> B strength = 1

```

BACKWARDS PRIMA FACIE REASONS

```

pf-reason 4: {} {C} ||=> ~R strength = 1
pf-reason 5: {} {B} ||=> C strength = 1

```

"))

yields the following set of *\*problems\**:

```

((1 (("P" nil 1) ("A" nil 1)) ("R" 1))
(("pf-reason 1" ("P" #<Compiled-function is-inference #x278A006>)) "Q" nil 1)
("pf-reason 2" ("Q" #<Compiled-function is-inference #x278A006>)) "R" nil 1)
("pf-reason 3" ("C" #<Compiled-function is-inference #x278A006>)) "~R" nil 1)
("pf-reason 4" ("B" #<Compiled-function is-inference #x278A006>)) "C" nil 1)
("pf-reason 5" ("A" #<Compiled-function is-inference #x278A006>)) "B" nil 1)
nil nil nil "This is a case of collective rebutting defeat")
(2 (("P" nil 1) ("A" nil 1)) ("R" 1))
(("pf-reason 1" ("P" #<Compiled-function is-inference #x278A006>)) "Q" nil 1)
("pf-reason 2" ("Q" #<Compiled-function is-inference #x278A006>)) "R" nil 1)
("pf-reason 3" ("A" #<Compiled-function is-inference #x278A006>)) "B" nil 1)
nil
(("pf-reason 4" nil ("C" nil)) ("~" "R" nil) nil 1)
("pf-reason 5" nil ("B" nil)) ("C" nil) nil 1)

```

```
nil "This is the same as #1 except that some reasons are backwards."))
```

When problems are entered in this form, the premises for forwards-reasons must be either pretty-formulas, or have the form  $\langle \text{pretty-formula} , \text{condition} \rangle$  where *condition* is either *inference*, *percept*, or *desire*. For example, we might construct a problem as follows:

```
(setf *problems* (make-problem-list
"Problem #1
This is a case of collective rebutting defeat
Given premises:
  P justification = 1
  A justification = 1
Ultimate epistemic interests:
  R interest = 1

FORWARDS PRIMA FACIE REASONS
pf-reason 1: {P , <Q , desire> , <R , percept>} ==> S strength = 1
pf-reason 4: {B} ==> C strength = 1
pf-reason 5: {A} ==> B strength = 1
"))
```

with the resulting problem

```
(1 (("P" nil 1) ("A" nil 1)) ("R" 1))
(("pf-reason 1"
 ("P" #<Compiled-function is-inference #x278A006>)
 ("Q" #<Compiled-function is-desire #x278A0F6>)
 ("R" #<Compiled-function is-percept #x278A1E6>))
 "S" nil 1)
 ("pf-reason 4" ("B" #<Compiled-function is-inference #x278A006>)) "C" nil 1)
 ("pf-reason 5" ("A" #<Compiled-function is-inference #x278A006>)) "B" nil 1)
 nil nil nil "This is a case of collective rebutting defeat")
```

Reasons can also contain variables, for use in pattern matching. For instance, here is a formulation of the paradox of the preface using variables:

```
Problem #15
Figure 18 -- the paradox of the preface.
Given premises:
(P1 a) justification = 1
(P2 a) justification = 1
(P3 a) justification = 1
(S a) justification = 1
(T a) justification = 1

Ultimate epistemic interests:
((Q1 a) & ((Q2 a) & (Q3 a))) interest = 1

FORWARDS PRIMA FACIE REASONS
pf-reason 1: {(P1 x)} ==> (Q1 x) variables = {x} strength = 1
pf-reason 2: {(P2 x)} ==> (Q2 x) variables = {x} strength = 1
pf-reason 3: {(P3 x)} ==> (Q3 x) variables = {x} strength = 1
pf-reason 4: {(S x)} ==> (R x) variables = {x} strength = 1
pf-reason 5: {(T x)} ==> ~((Q1 x) & ((Q2 x) & (Q3 x))) variables = {x} strength = 1
pf-reason 6: {(S1 x)} ==> ((T x) @ ~((Q1 x) & ((Q2 x) & (Q3 x)))) variables = {x} strength = 1
pf-reason 7: {(S2 x)} ==> ((T x) @ ~((Q1 x) & ((Q2 x) & (Q3 x)))) variables = {x} strength = 1
pf-reason 8: {(S3 x)} ==> ((T x) @ ~((Q1 x) & ((Q2 x) & (Q3 x)))) variables = {x} strength = 1

FORWARDS CONCLUSIVE REASONS
con-reason 1: {(Q1 x) , (Q2 x)} ==> ((Q1 x) & (Q2 x)) variables = {x} strength = 1
con-reason 2: {(Q2 x) , (Q3 x)} ==> ((Q2 x) & (Q3 x)) variables = {x} strength = 1
con-reason 3: {(Q1 x) , (Q3 x)} ==> ((Q1 x) & (Q3 x)) variables = {x} strength = 1
con-reason 4: {(R x) , ((Q1 x) & (Q3 x))} ==> (S2 x) variables = {x} strength = 1
con-reason 5: {(R x) , ((Q2 x) & (Q3 x))} ==> (S1 x) variables = {x} strength = 1
con-reason 6: {(R x) , ((Q1 x) & (Q2 x))} ==> (S3 x) variables = {x} strength = 1
```

con-reason 7:  $\{((Q1\ x) \ \& \ (Q2\ x)) , \ \sim((Q1\ x) \ \& \ ((Q2\ x) \ \& \ (Q3\ x)))\} \ ||\Rightarrow \ \sim(Q3\ x)$  variables = {x}  
strength = 1  
con-reason 8:  $\{((Q2\ x) \ \& \ (Q3\ x)) , \ \sim((Q1\ x) \ \& \ ((Q2\ x) \ \& \ (Q3\ x)))\} \ ||\Rightarrow \ \sim(Q1\ x)$  variables = {x}  
strength = 1  
con-reason 9:  $\{((Q1\ x) \ \& \ (Q3\ x)) , \ \sim((Q1\ x) \ \& \ ((Q2\ x) \ \& \ (Q3\ x)))\} \ ||\Rightarrow \ \sim(Q2\ x)$  variables = {x}  
strength = 1

**BACKWARDS CONCLUSIVE REASONS**

con-reason 11:  $\{ \} \{ (Q1\ x) , (Q2\ x) , (Q3\ x) \} \ ||\Rightarrow \ ((Q1\ x) \ \& \ ((Q2\ x) \ \& \ (Q3\ x)))$  variables = {x}  
strength = 1

To expedite constructing problems in this latter form, the user may find it useful to cut and paste the following template for a single problem:

**Problem #1**

description of problem

Given premises:

- P justification = 1
- P justification = 1
- P justification = 1
- P justification = 1
- P justification = 1

Ultimate epistemic interests:

- R interest = 1
- R interest = 1
- R interest = 1

**FORWARDS PRIMA FACIE REASONS**

pf-reason 1:  $\{P , P , P\} \ ||\Rightarrow \ Q$  variables = {x , y , z} strength = 1  
pf-reason 1:  $\{P , P , P\} \ ||\Rightarrow \ Q$  variables = {x , y , z} strength = 1  
pf-reason 1:  $\{P , P , P\} \ ||\Rightarrow \ Q$  variables = {x , y , z} strength = 1  
con-reason 1:  $\{<P , condition> , <P , condition>\} \ ||\Rightarrow \ Q$  variables = {x , y , z} strength = 1  
con-reason 1:  $\{<P , condition> , <P , condition>\} \ ||\Rightarrow \ Q$  variables = {x , y , z} strength = 1

**FORWARDS CONCLUSIVE REASONS**

con-reason 1:  $\{P , P , P\} \ ||\Rightarrow \ Q$  variables = {x , y , z} strength = 1  
con-reason 1:  $\{P , P , P\} \ ||\Rightarrow \ Q$  variables = {x , y , z} strength = 1  
con-reason 1:  $\{P , P , P\} \ ||\Rightarrow \ Q$  variables = {x , y , z} strength = 1  
con-reason 1:  $\{<P , condition> , <P , condition>\} \ ||\Rightarrow \ Q$  variables = {x , y , z} strength = 1  
con-reason 1:  $\{<P , condition> , <P , condition>\} \ ||\Rightarrow \ Q$  variables = {x , y , z} strength = 1

**BACKWARDS PRIMA FACIE REASONS**

pf-reason 2:  $\{P , P , P\} \{Q , Q , Q\} \ ||\Rightarrow \ R$  variables = {x , y , z} strength = 1  
pf-reason 2:  $\{P , P , P\} \{Q , Q , Q\} \ ||\Rightarrow \ R$  variables = {x , y , z} strength = 1  
pf-reason 2:  $\{P , P , P\} \{Q , Q , Q\} \ ||\Rightarrow \ R$  variables = {x , y , z} strength = 1  
pf-reason 2:  $\{P , P , P\} \{Q , Q , Q\} \ ||\Rightarrow \ R$  variables = {x , y , z} strength = 1  
pf-reason 2:  $\{P , P , P\} \{Q , Q , Q\} \ ||\Rightarrow \ R$  variables = {x , y , z} strength = 1

**BACKWARDS CONCLUSIVE REASONS**

con-reason 2:  $\{P , P , P\} \{Q , Q , Q\} \ ||\Rightarrow \ R$  variables = {x , y , z} strength = 1  
con-reason 2:  $\{P , P , P\} \{Q , Q , Q\} \ ||\Rightarrow \ R$  variables = {x , y , z} strength = 1  
con-reason 2:  $\{P , P , P\} \{Q , Q , Q\} \ ||\Rightarrow \ R$  variables = {x , y , z} strength = 1  
con-reason 2:  $\{P , P , P\} \{Q , Q , Q\} \ ||\Rightarrow \ R$  variables = {x , y , z} strength = 1  
con-reason 2:  $\{P , P , P\} \{Q , Q , Q\} \ ||\Rightarrow \ R$  variables = {x , y , z} strength = 1

This template is contained in the file "Template".

A precompiled version of a problem-set can be produced by first printing the contents of *\*problems\**, producing a display like the following:

```

((1 ("P" nil 1) ("A" nil 1)) ("R" 1))
  ("pf-reason 1" ("P" #<Compiled-function is-inference #x278A006>)) "Q" nil 1)
  ("pf-reason 2" ("Q" #<Compiled-function is-inference #x278A006>)) "R" nil 1)
  ("pf-reason 3" ("C" #<Compiled-function is-inference #x278A006>)) "~R" nil 1)
  ("pf-reason 4" ("B" #<Compiled-function is-inference #x278A006>)) "C" nil 1)
  ("pf-reason 5" ("A" #<Compiled-function is-inference #x278A006>)) "B" nil 1))
nil nil nil "This is a case of collective rebutting defeat")
(2 ("P" nil 1) ("A" nil 1)) ("R" 1))
  ("pf-reason 1" ("P" #<Compiled-function is-inference #x278A006>)) "Q" nil 1)
  ("pf-reason 2" ("Q" #<Compiled-function is-inference #x278A006>)) "R" nil 1)
  ("pf-reason 3" ("A" #<Compiled-function is-inference #x278A006>)) "B" nil 1))
nil
  ("pf-reason 4" nil ("C" nil)) ("~" "R") nil nil 1)
  ("pf-reason 5" nil ("B" nil)) ("C" nil) nil 1))
nil "This is the same as #1 except that some reasons are backwards.")

```

The next step is to replace the terms for the compiled functions by the corresponding expressions “desire”, “percept”, and “inference”, thus producing:

```

((1 ("P" nil 1) ("A" nil 1)) ("R" 1))
  ("pf-reason 1" ("P" inference)) "Q" nil 1)
  ("pf-reason 2" ("Q" inference)) "R" nil 1)
  ("pf-reason 3" ("C" inference)) "~R" nil 1)
  ("pf-reason 4" ("B" inference)) "C" nil 1)
  ("pf-reason 5" ("A" inference)) "B" nil 1))
nil nil nil "This is a case of collective rebutting defeat")
(2 ("P" nil 1) ("A" nil 1)) ("R" 1))
  ("pf-reason 1" ("P" inference)) "Q" nil 1)
  ("pf-reason 2" ("Q" inference)) "R" nil 1)
  ("pf-reason 3" ("A" inference)) "B" nil 1))
nil
  ("pf-reason 4" nil ("C" nil)) ("~" "R") nil nil 1)
  ("pf-reason 5" nil ("B" nil)) ("C" nil) nil 1))
nil "This is the same as #1 except that some reasons are backwards.")

```

Then enclose the result in the following expression:

```
(setf *problems (quote ... ))
```

The files *Problems-sl.lsp* and *Problems-Q.lsp* were produced in this way. The advantage of using pre-compiled problem-sets is that they load much more quickly.